

Name: \_\_\_\_\_

Problem	Points	Score
1(a)	15	
1(b)	15	
2(a)	10	
2(b)	10	
2(c)	5	
2(d)	5	
2(e)	10	
3(a)	15	
3(b)	15	
Total	100	

## Notes:

- (1) The exam is closed books and notes except for one double-sided sheet of notes.
- (2) Please indicate clearly your answer to the problem.
- (3) If I can't read or follow your solution, it is wrong and no partial credit will be awarded.

**Problem No. 1:** Consider the LTCC difference equation:  $y[n] = 0.5y[n - 2] + 0.25x[n - 1]$ . Assume the initial conditions are zero.

(a) Find the impulse response.

(b) Is the system stable? Justify your answer using a technique that does not depend on your answer to (a).

**Problem No. 2:** Students at Temple are graded on a 5 point scale: A,B,C,D, and F. The Registrar, a former graduate of ECE 4522, decides to put this class to good use by developing a program to model the fluctuation of the average GPA at the university. The model the Registrar uses predicts the average GPA for the current year as a function of the number of students enrolled at the beginning of the first semester, the unemployment rate on Jan. 1 of the current year, and the size of the US population for the year corresponding to the current year minus 18 years.

(a) Write an equation that represents a model of this signal.

Is the signal described above (circle all that apply):

one dimensional

multidimensional

single channel

multichannel

continuous

discrete-time

continuous in amplitude digital in amplitude

(b) What is the Nyquist rate for the signal:  $x(n) = (\sin 2\pi 1000t + 7.5\pi)^2$

(c) Given the signal,  $x(t) = \begin{cases} (-\frac{1}{2})^{1000t} & |t| < 0.0015 \text{ secs} \\ 0 & \text{elsewhere} \end{cases}$ , compute the value of  $x(t)$  at  $t = 0.002 \text{ secs}$  by sampling at  $f_s = 1000 \text{ Hz}$ , upsampling the signal to a new sample frequency of  $f_s = 2000 \text{ Hz}$ , and evaluating this new discrete signal at  $n = 4$  (which corresponds to  $t = 0.002 \text{ secs}$ ).

(d) Why is the answer to (c) not equal to  $x(t)$  evaluated at  $t = 0.002 \text{ secs}$ ?

(e) In class, we discussed that a standard DVD disc can hold about 2 Gbytes of data. How many minutes of digital audio can this disc hold? Be careful to explain and justify any assumptions you make in your answer.

**Problem No. 3:** For the signal,  $x[n] = \{1, 0, 1, 0\}$  and the impulse response,  $h[n] = \{0, 1, 0, 1\}$ :

(a) Compute the output,  $y[n]$ .

(b) Is the system causal? stable? Time-invariant? Explain.