

## Lecture 40

"The Discrete-Time Version of Signals"



(1) A/D conversion:

The Nyquist Theorem

$f_s \rightarrow 2f_{max}$

Spectrum of the sampled signal

Sinc Interpolator

Quantization: Linear/Uniform

Non-linear/logarithmic

Signal Dither

Linear: SNR  $\propto$  GB (B is # of bits)

(2) Systems:

"Engineering is all about modeling"

systems as differential equations"

Continuous time

diff. eq.

$\Leftrightarrow$  discrete-time

differential equations

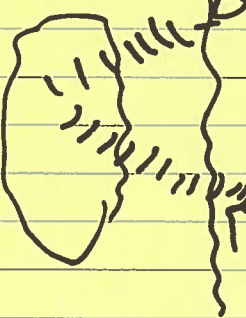
Linear constant coefficient difference eq.

$\rightarrow$  LCCD

Linearity and Time-Invariance (LTI)

$$x(n) = \delta(n)$$

$$y(n) = h(n)$$



$$h(n) \Rightarrow H(z)$$

Convolution

Direct Difference Eq. computation

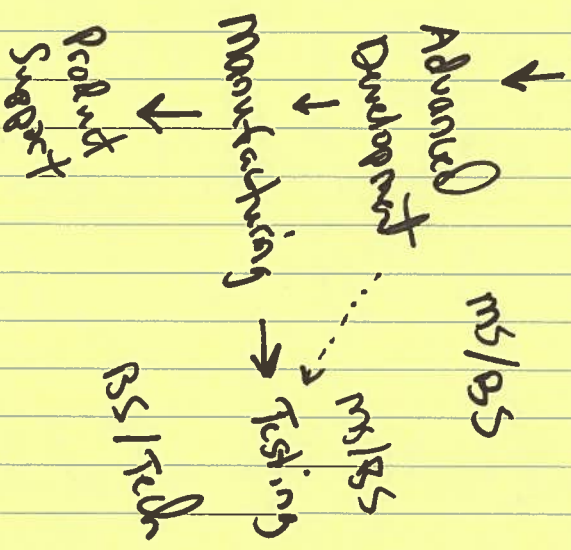
Causality ( $h(n) = 0 \quad n < 0$ )

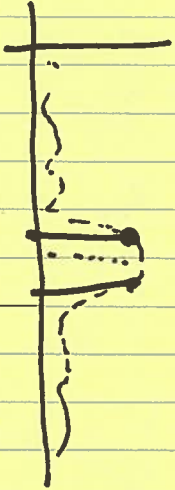
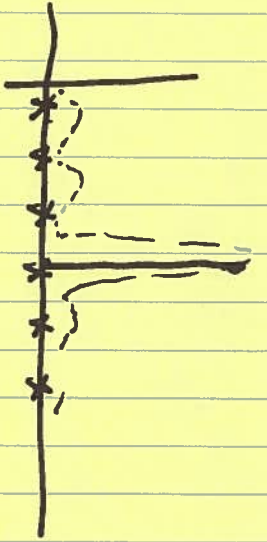
Stability (poles must be inside the unit circle)

# Digital Filter Realizations

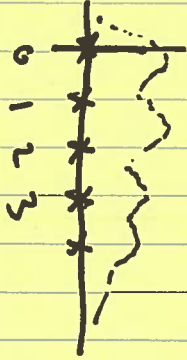
Direct Form  
Canonical I & II

Aside: Research PhD or MS





$f_3 = 10$   
 $N = 10$



$\{x_1, x_2, \dots, x_n\}$

$n = 11$

$$f_2 = \frac{p}{11}$$

$\{x_1, x_2, \dots, x_n\}$